

Square of an Enormously Large Number

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Abstract- In this world of extremely fast and effective manipulations and calculations, the requirements for the time taken by a computation needs to be nailed down to the extreme low as possible. The time required for calculations doesn't come up as an issue unless you type in a really huge number, like a number including 100-digits or so. When this kind of number is required to be processed upon, our computer systems take quite a while to process upon the operations being performed on the number. A process for quick and easily manipulated computations is required to be produced, in order to increase the productivity, convenience, ease of use and fairly deal with budgetary concerns. This document provides general practices, procedures and tools for creating a faster computation of square of extremely large numbers. It is aimed for engineers, Mathematical gurus, algorithm geeks, who are assumed to possess basic knowledge regarding *what is meant by square of a number*. It addresses basic knowledge about how to calculate the square using conventional means and how the improvement can be made to save time.

Keywords— *Square of a number, Time-Complexity, Algorithm Design*

I. INTRODUCTION

Let's start with basics of exponentiation. Exponentiation can be referred to as the procedure of multiplying a given number 'n' by itself for 'm'-number of times. The number to be multiplied by itself can be called as 'base', i.e. 'n' here is 'base', while the number *how many times it is to be multiplied*, can be called as 'exponent', i.e. 'm' here is 'exponent'. The symbol required to represent the exponentiation can be given as '^', called as "carat". Thus, exponentiation can now be shown in mathematical terms as 'n ^ m', also called as 'n to the power m'.

This simple concept of multiplication of a number by itself has played a very significant role in the world of mathematics. Polynomials are all based upon the base-exponent relationship of variables. These polynomials build up the infrastructure of Algebra.

When the exponent is made to be nothing but 2 (*two*), the exponentiation starts to be termed as calculating the square of a number. Now, the base 'n' becomes a k-digit number and 'm' becomes 2. This is represented as n^2 and termed as 'n to the power two' or in more familiar words 'square of n'. From calculating the area of a circle, to equating popular Energy-mass equation of Albert Einstein, the exponentiation has developed its way through into being one of the very crucial parts of the whole mathematics.

In Computer Technology, the requirements for developing a faster way of computing the square of a given number have evolved from various methods to various others. There exist many of them that are effective enough to compute the

square of very large numbers, but they are not as efficient as the method we are about to discuss.

After having gone through this paper, you will be able to calculate the square of a given number with an ease never mentioned before and the algorithm discussed here would provide an extremely fast way of computing the squares of an extremely large number, i.e. consisting of several hundred digits.

II. CONVENTIONAL METHOD

A. N to the power two

A very convenient method, as the name suggests is to multiply the number with itself. For example, if we have a number 'n' equals to 45 and it is supposed to be calculated square of, then we need to multiply 45 with itself, i.e. 45, in order to get the result 2025, as the square of this number. In this approach, it is to be understood what it actually means to multiply a number.

B. Multiplying a number

What it actually means to have a number multiplied is adding the number as many times as the number it is required to be multiplied with. Considering the previous example, 45^2 depicts that 45 is to be multiplied with 45 and in order to multiply 45 with another 45, it would have to be added with itself 45 times, i.e. $45 + 45 + 45 + \dots + 45$ (45 times).

The square of a number can thus be calculated in this manner. But, it can be easily seen how hectic this procedure becomes when a number of sufficiently large number of

digits is encountered. This conventional approach is the basic and the most absolute approach but computer technology requires a faster way.

III. DEVELOPING A MEANS

It has to be seen how the advancement in computer technology has brought the computational time to almost negligible amount. The programming language used here is Python and the module to keep track of the time element is 'time'. Recursive calling of function has been used in order to keep the complexity of the algorithm as low as possible.

A. Time module of Python

This module can be used in order to keep track of the time taken by a particular instruction or a set of instructions in order to build up an exact scenario of how long does an instruction or a set of instructions take to execute. This can be shown to be done as:

```
time1 = time.time()
# Your instructions go here
time2 = time.time()
time2 = time2 - time1
```

It is clear that a variable called 'time1' holds the time instance that occurred just before instructions had started executing and 'time2' holds the time instance that occurred right after the execution of instructions was done. Subtracting the first variable from second gives the time required by the set of instructions to execute. In order to use this module, programmer has to import the module exclusively.

B. Recursion

Recursion can be defined as the way in which one method keeps passing a lower set of parameters to itself until a base case is encountered in which function returns primitive values that are predefined in the function or are too obvious to guess. Recursion in this manner can be thought of as a way in programming languages by which one method makes a call to itself with a lower set of values. This can be represented as:

```
def meth( param1, param2, ... , paramk ):
    # here goes the base case
    meth( param_smaller1, param_smaller2, ... ,
param_smallerk )
```

It is clear from the example above that 'meth' method is calling itself with lower set of values.

IV. GIVING THE ALGORITHM

A. Algorithm

Algorithm defines a set of sequential rules required to be followed in order to solve a particular problem. The algorithm for calculating the square of a given number can be given as:

1. *if the number is 1-digit, then*
2. *return the square of number*
3. *if modulo-10 of the number is 0, then*
4. *recursively call the algorithm over 1/10th of the number*
5. *return the result obtained after multiplying it with 100 or appending two zeroes at the end of the result*
6. *else*
7. *compute the nearest but smaller number that is exactly divisible by 10, save it in variable 'num'*
8. *recurse over the obtained number and store the result in a variable, say 'sq'*
9. *i = 1*
10. *while units digit of the number is greater than 0*
11. *sq = sq + num * 2 + i*
12. *increase i by 2*
13. *decrease units digit of the number by 1*
14. *return sq*

Above algorithm can be explained in the following manner:

Line 1 is the base case for the recursive algorithm, i.e. whenever the length of the number is 1, it should simply return the square of the number. This can be done as simple multiplication of the number by itself or by listing every single case from 0 to 9 and returning the corresponding value.

Now, there may occur two cases, i.e. when the number is exactly divisible by 10 and when the number is not exactly divisible by 10. When the number is exactly divisible by 10, then it is known by practice that the square of this number

will be divisible by 100. Thus, we now only need to find the square of the 1/10th of the number, and when the result comes, we will multiply it with 100 for the correct answer. In programming language that support string operations, that most of the programming languages do, two zeroes can be appended at the end of the result obtained. This implementation can be pointed out in the algorithm on line 3, 4 and 5.

In *line 3*, modulo-10 of the number is checked. If it is found to be zero, a recursive call on 1/10th of the number is made and the result is simply returned back.

When the number is found to be not divisible by 10 and leaves a remainder, this remainder can be stored back for further utilization. Compute the nearest but smaller 10's multiple of the number as done in *line 7*. Recursive call can be made over this number and the result is to be stored in a variable, say 'sq'. This is done in *line 8*.

In *line 9*, a variable called 'i' is assigned a value of 1. The loop on *line 10* sustains until the remainder that we had previously stored is greater than zero.

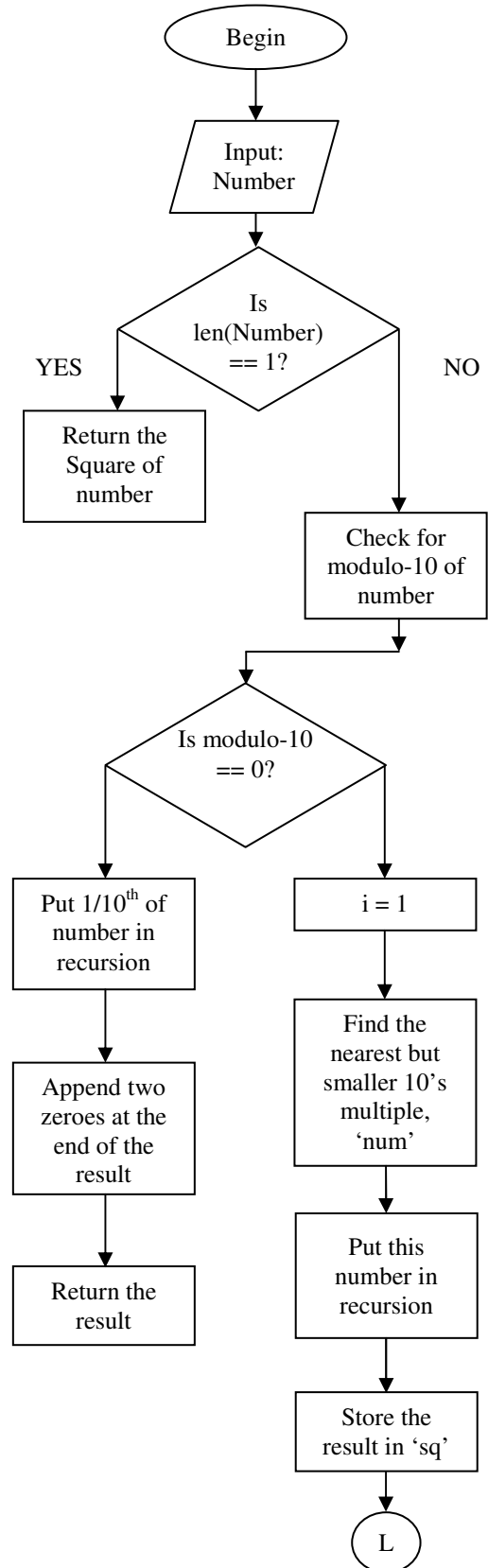
The main part of this whole algorithm resides in the next three lines from *line 11* to *line 13*. The explanation for this can be stated by an example.

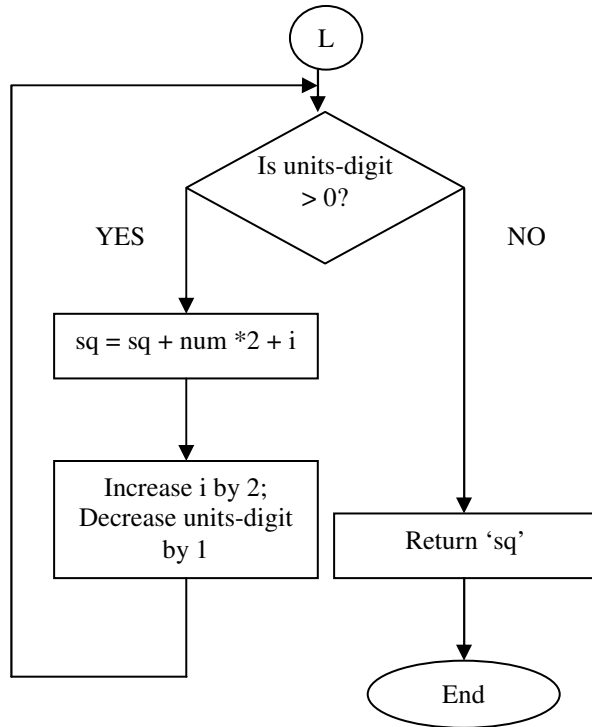
Let's consider a number, 34. The nearest but smaller 10's multiple to this number is 30. Square of 30 can be calculated using recursive calls as described above. In order to calculate the square of 34, four iterations are carried out inside the while loop. In first iteration, square of 30, i.e. 900, is added up with 'twice of 30' and 1, to yield the square of 31 as 961. In second iteration, 961 is added up with 'twice of 30' and 3, to yield 1024, i.e. the square of 32. In the next iteration, 1024 is added up with 'twice of 30' and 5, to yield the square of 33 as 1089. In the fourth iteration, 1089 is added up with 'twice of 30' and 7 to give the final answer of square of 34, i.e. 1156.

Thus, it can be shown that the algorithm applies to all sort of inputs and returns the square of number in recursive manner.

The square calculated can be returned as in *line 14*.

B. Flowchart





C. Corectness of the Algorithm

Correctness of the algorithm can be proved by having proved the applicability of the algorithm over all sort of inputs that the algorithm claims to be working upon. This is where the working of the inner of the 'while' loop is explained.

This method of computing the square of a number can also be implemented in thought process for human beings for faster calculation of square of small numbers.

Let's consider a number, 57. The requirement is to find the square of this number. The unit's digit being 7 is required to be stored in a variable, say 'udigit'. The nearest but smaller 10's multiple is found to be 50. Calculate the square of 50. The square of 50 can be easily calculated as two zeroes are required to be placed after the square of 5. This is done in the first recursion in the algorithm given above. This ensures that the square of a number ending with a zero is calculated by eliminating the zero in the end and calculating the square of the remaining number by recursion and multiplying the result by 100 (or placing two zeroes in the end of the result in thought process).

Once the square of 50 is calculated as 2500, the while loop gets activated and the processing is done as follows:

In the first iteration, add $50 * 2 = 100$ and 1 to 2500, to make it 2601, this is the square of 51. In the second iteration, add $50 * 2$ and 3 to 2601, to make it 2704, this is the square of 52. By proof of induction it can be shown that

proceeding in this manner, the square of a number can be calculated with faster pace and greater ease.

D. Implementation

Every algorithm is required to have a working model in order to test the applicability and complexity of it. The following program is written in Programming language and gives a working model of the algorithm given here.

import time

num = 99999

time1 = time.time()

def func(num):

if num == 0:
return 0

if num == 1:
return 1

if num == 2:
return 4

if num == 3:
return 9

if num == 4:
return 16

if num == 5:
return 25

if num == 6:
return 36

if num == 7:
return 49

if num == 8:
return 64

if num == 9:
return 81

num1 = num % 10

if num1 == 0:

```

num2 = num / 10

num3 = func(num2) * 100

return num3

else:

num2 = num - num1
num3 = func(num2)

sq = num3
i = 1

while num1 > 0:

    sq = sq + num2 * 2 + i

    i += 2

    num1 -= 1

return sq

time2 = time.time()

time2 = time2 - time1

print "***ALGORITHM USED***"

print "The square of ", num, " is: ", sq
print "Time required: ", time2, " and size of input: ",
len(str(num))

time3 = time.time()

num1 = num ** 2

time4 = time.time()

time4 = time4 - time3

print "***CONVENTIONAL METHOD***"
print "The square of ", num, " is: ", num1
print "Time required: ", time4, " and size of input: ",
len(str(num))

```

It should be clear from the program given above that time module of Python language has been used in order to compare the time taken by each of the two methods: first, method given by the algorithm mentioned afore and second, the conventional method of squaring a number.

E. Observation

Following screenshots show the time difference taken when the square of a sufficiently large number is calculated. We start with a number consisting of 10 digits and proceed by increasing the number by 10 digits every time.

```

***ALGORITHM USED***
The square of 9987476453 is: 99749685899229461209
Time required: 1.90734863281e-06 and size of the input: 10
***CONVENTIONAL METHOD***
The square of 9987476453 is: 99749685899229461209
Time required: 5.96046447754e-06 and size of the input: 10
>python square.py
***ALGORITHM USED***
The square of 99874764536457329810 is: 9974968591212794709474296386875114636100
Time required: 2.14576721191e-06 and size of the input: 20
***CONVENTIONAL METHOD***
The square of 99874764536457329810 is: 9974968591212794709474296386875114636100
Time required: 9.05990600586e-06 and size of the input: 20
>python square.py
***ALGORITHM USED***
The square of 998747645364573298106347520010 is: 9974968591212794709601087800152954
89119643180972277350400100
Time required: 1.90734863281e-06 and size of the input: 30
***CONVENTIONAL METHOD***
The square of 998747645364573298106347520010 is: 9974968591212794709601087800152954
89119643180972277350400100
Time required: 6.91413879395e-06 and size of the input: 30
>

```

```

>python square.py
***ALGORITHM USED***
The square of 9987476453645732981063475200106457832009 is: 997496859121279470960108
78001658543802227292535610492442026008623596056464976081
Time required: 2.14576721191e-06 and size of the input: 40
***CONVENTIONAL METHOD***
The square of 9987476453645732981063475200106457832009 is: 997496859121279470960108
78001658543802227292535610492442026008623596056464976081
Time required: 6.91413879395e-06 and size of the input: 40
>python square.py
***ALGORITHM USED***
The square of 99874764536457329810634752001064578320096234500955 is: 99749685912127
94709601087800165854380223974592190815130912643167020619297046714685670374057895912025
Time required: 1.90734863281e-06 and size of the input: 50
***CONVENTIONAL METHOD***
The square of 99874764536457329810634752001064578320096234500955 is: 99749685912127
94709601087800165854380223974592190815130912643167020619297046714685670374057895912025
Time required: 7.86781311035e-06 and size of the input: 50
>

```

```

>python square.py
***ALGORITHM USED***
The square of 998747645364573298106347520010645783200962345009556455599932 is: 9974
96859121279470960108780016585438022397459219094408121727318101058858410229366754152022
228104758964713471682038404624
Time required: 2.14576721191e-06 and size of the input: 60
***CONVENTIONAL METHOD***
The square of 998747645364573298106347520010645783200962345009556455599932 is: 9974
96859121279470960108780016585438022397459219094408121727318101058858410229366754152022
228104758964713471682038404624
Time required: 8.10623168945e-06 and size of the input: 60
>python square.py
***ALGORITHM USED***
The square of 9987476453645732981063475200106457832009623450095564555999328456700991
is: 99749685912127947096010878001658543802239745921909440812172900732309932111094264
437165119511220982807459651088203491310320394443891180382081
Time required: 2.14576721191e-06 and size of the input: 70
***CONVENTIONAL METHOD***
The square of 9987476453645732981063475200106457832009623450095564555999328456700991
is: 99749685912127947096010878001658543802239745921909440812172900732309932111094264
437165119511220982807459651088203491310320394443891180382081
Time required: 8.10623168945e-06 and size of the input: 70
>

```



```

654798760 is: 9974968591212794709601087800165854380223974592190944081217290073230994
74015187390164759800583796714205927071801142700820102833966131866195735054736725609753
7600
Time required: 1.90734863281e-06 and size of the input: 80
***CONVENTIONAL METHOD***
The square of 99874764536457329810634752001064578320096234500955645559993284567009917
654798760 is: 9974968591212794709601087800165854380223974592190944081217290073230994
74015187390164759800583796714205927071801142700820102833966131866195735054736725609753
7600
Time required: 8.10623168945e-06 and size of the input: 80
>python square.py
***ALGORITHM USED***
The square of 99874764536457329810634752001064578320096234500955645559993284567009917
65479876063409556675467833454 is: 997496859121279470960108780016585438022397459219094408121729
0073230994740151874028307888841385913855345764231669432594556939685004421878139117987
92291817215097953917710859414889
Time required: 2.14576721191e-06 and size of the input: 90
***CONVENTIONAL METHOD***
The square of 99874764536457329810634752001064578320096234500955645559993284567009917
65479876063409556675467833454 is: 997496859121279470960108780016585438022397459219094408121729
0073230994740151874028307888841385913855345764231669432594556939685004421878139117987
92291817215097953917710859414889
Time required: 9.05990600586e-06 and size of the input: 90

```

```

>python square.py
***ALGORITHM USED***
The square of 99874764536457329810634752001064578320096234500955645559993284567009917
65479876063409556675467833454 is: 997496859121279470960108780016585438022397459219094408121729
0073230994740151874028307888841385913855345764231669432594556939685004421878139117987
92291817215097953917710859414889
Time required: 1.90734863281e-06 and size of the input: 100
***CONVENTIONAL METHOD***
The square of 99874764536457329810634752001064578320096234500955645559993284567009917
65479876063409556675467833454 is: 997496859121279470960108780016585438022397459219094408121729
0073230994740151874028307888841385913855345764231669432594556939685004421878139117987
92291817215097953917710859414889
Time required: 1.31130218506e-05 and size of the input: 100

```

```

>python square.py
***ALGORITHM USED***
The square of 998747645364573298106347520010645783200962345009556455599932845670099176547987606340955667546
78334549987476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
997476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
9974968591212794709601087800165854380223974592190944081217290073230994740151874028307888841385913855345764231669432594556939685004421878139117987
92291817215097953917710859414889
Time required: 1.90734863281e-06 and size of the input: 300
***CONVENTIONAL METHOD***
The square of 998747645364573298106347520010645783200962345009556455599932845670099176547987606340955667546
78334549987476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
997476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
9974968591212794709601087800165854380223974592190944081217290073230994740151874028307888841385913855345764231669432594556939685004421878139117987
92291817215097953917710859414889
Time required: 2.14576721191e-06 and size of the input: 90
***CONVENTIONAL METHOD***
The square of 9987476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
997476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
9974968591212794709601087800165854380223974592190944081217290073230994740151874028307888841385913855345764231669432594556939685004421878139117987
92291817215097953917710859414889
Time required: 2.14576721191e-06 and size of the input: 90
***CONVENTIONAL METHOD***
The square of 9987476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
997476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
9974968591212794709601087800165854380223974592190944081217290073230994740151874028307888841385913855345764231669432594556939685004421878139117987
92291817215097953917710859414889
Time required: 1.31130218506e-05 and size of the input: 100

```

```

***ALGORITHM USED***
The square of 998747645364573298106347520010645783200962345009556455599932845670099176547987606340955667546
78334549987476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
997476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
9974968591212794709601087800165854380223974592190944081217290073230994740151874028307888841385913855345764231669432594556939685004421878139117987
92291817215097953917710859414889
Time required: 1.90734863281e-06 and size of the input: 400
***CONVENTIONAL METHOD***
The square of 998747645364573298106347520010645783200962345009556455599932845670099176547987606340955667546
78334549987476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
997476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
9974968591212794709601087800165854380223974592190944081217290073230994740151874028307888841385913855345764231669432594556939685004421878139117987
92291817215097953917710859414889
Time required: 2.14576721191e-06 and size of the input: 400
***CONVENTIONAL METHOD***
The square of 998747645364573298106347520010645783200962345009556455599932845670099176547987606340955667546
78334549987476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
997476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
9974968591212794709601087800165854380223974592190944081217290073230994740151874028307888841385913855345764231669432594556939685004421878139117987
92291817215097953917710859414889
Time required: 1.31130218506e-05 and size of the input: 400

```

It can be easily seen how the algorithm works in constant time without having the effect of the number of digits in the number whose square is required to be calculated. This becomes interesting when it is seen that the algorithm consumes much less time required to compute the square than the conventional technique of using exponential operation.

The algorithm also works for very large number, say numbers consisting of 100 digits and more. The time consumed to compute the square of the number remains constant and can be shown in the following screenshots that show how the impact of number of digits doesn't affect the running time of the algorithm, but it does affect the conventional method of exponential operation.

```

>python square.py
***ALGORITHM USED***
The square of 99874764536457329810634752001064578320096234500955645559993284567009917
6547987606340955667546783345499874764536457329810634752001064578320096234500955645559993284567009917
65479876063409556675467833454 is: 9974968591212794709601087800165854380223974592190944081217290073230994740151874028307888841385913855345764231669432594556939685004421878139117987
92291817215097953917710859414889
Time required: 2.14576721191e-06 and size of the input: 200
***CONVENTIONAL METHOD***
The square of 99874764536457329810634752001064578320096234500955645559993284567009917
6547987606340955667546783345499874764536457329810634752001064578320096234500955645559993284567009917
65479876063409556675467833454 is: 9974968591212794709601087800165854380223974592190944081217290073230994740151874028307888841385913855345764231669432594556939685004421878139117987
92291817215097953917710859414889
Time required: 1.50203704834e-05 and size of the input: 200

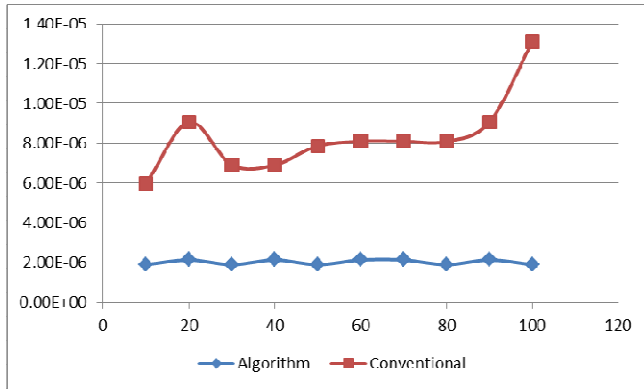
```

```

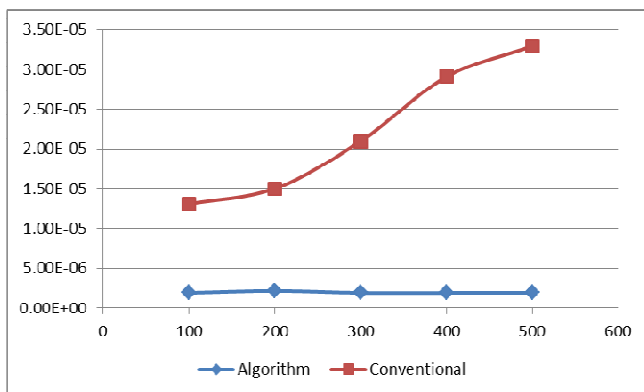
>python square.py
***ALGORITHM USED***
The square of 99874764536457329810634752001064578320096234500955645559993284567009917654798760634095566754678334549987476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
997476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
9974968591212794709601087800165854380223974592190944081217290073230994740151874028307888841385913855345764231669432594556939685004421878139117987
92291817215097953917710859414889
Time required: 1.90734863281e-06 and size of the input: 500
***CONVENTIONAL METHOD***
The square of 99874764536457329810634752001064578320096234500955645559993284567009917654798760634095566754678334549987476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
997476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
9974968591212794709601087800165854380223974592190944081217290073230994740151874028307888841385913855345764231669432594556939685004421878139117987
92291817215097953917710859414889
Time required: 2.14576721191e-06 and size of the input: 500
***CONVENTIONAL METHOD***
The square of 99874764536457329810634752001064578320096234500955645559993284567009917654798760634095566754678334549987476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
997476453645732981063475200106457832009623450095564555999328456700991765479876063409556675467833454
9974968591212794709601087800165854380223974592190944081217290073230994740151874028307888841385913855345764231669432594556939685004421878139117987
92291817215097953917710859414889
Time required: 1.50203704834e-05 and size of the input: 500

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It is clearly seen in the above pictures that the square calculated through the algorithm mentioned in this paper takes reasonably less amount of time than the conventional method of calculating the square. A clear vision of the time taken can be deciphered by presenting a graph holding the amount of time taken on Y-axis with respect to the number of digits of the number on X-axis.



In the graph shown below, the comparison of number of digits with respect to the time taken for calculating the square of a number by both the methods is shown. It can be seen how the time taken increases with the increase in number of digits. It should be noted here that input numbers are reasonably large, i.e. consisting of 100, 200, 300, 400 and 500 digits.



F. Advancement in the Algorithm

The algorithm can also be modified for the computation of higher exponential powers. This can be achieved by strategically repeating the algorithm until the required result is obtained. A more elaborative explanation for this fact can be given by an example.

Let a base number be '46' and the exponent be '9'. The operation 46^9 is required to be carried out. This can be done by calculating the square of 46 using the algorithm. This gives 46^2 . Calculating the square of the result obtained will give 46^4 . Applying the same algorithm again for calculating the square will give 46^8 . Now, this result is simply required to be multiplied by another 46 in order to yield the result for 46^9 . In this manner, higher exponential operations on a number can be dealt with.

G. Future Scope

1. The algorithm being used here functions on a pre-determined set of hardware that keeps it working in a conventional way of execution of operations that limits the effectiveness of the algorithm. The speed of calculation can be improved by providing the algorithm with proper hardware. With proper hardware capable of holding the variables and function and heaps used, the algorithm can be proved to be even faster.
2. It can be seen from the fact of execution of the algorithm, that for all the numbers, the nearest but smaller 10's multiple is calculated. For numbers that are more than 5 units more to the 10's multiple, i.e. 57 is 50 (10's multiple) + 7 (unit's digit), the inner loop executes for seven times. This can be reduced by having considered the nearest but larger 10's multiple, i.e. 60 for 57. Now, square of 60 can be calculated as 3600 and twice of 60 can be subtracted from 3600 and 1 is added to get the square of 59, i.e. 3481. In order to find the square of 58, from 3481, twice of 60 has to be subtracted again and 3 has to be added up to the result, to get 3364. In the next iteration, subtracting twice of 60 from 3364 and adding 5 will give the square of 57, as 3249. This reduces the number of iterations from 7 to 3 and thus leads to a better and efficient method of calculating the squares.

V. CONCLUSION

The requirements for computing the square of a given number faster than presently used conventional method have been fulfilled. It can now be concluded that a square of a number can be subjected to be considered as a problem that can be solved by dividing the problem into sub-problem of calculating the square of the nearest but smaller 10's multiple of the given number. This implementation is done in programming by using the concept of recursion.

VI. ACKNOWLEDGMENT

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VII. REFERENCES

I would mention here that this discovery is individual to the author only and contribution of no other person or any source is involved. The following references contribute to the development of the program and not the algorithm:

- [1] Dive Into Python, Mark Pilgrim, Published 20th May 2004